Lecture 6

Register Allocation

- I Introduction
- II Abstraction and the Problem
- III Algorithm

Reading: Chapter 8.8.4

Before next class: Chapter 10.1 - 10.2

Advanced Compilers M. Lam

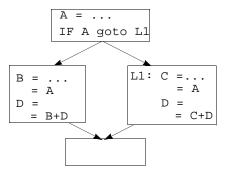
I. Motivation

- Problem
 - Allocation of variables (pseudo-registers) to hardware registers in a procedure
- Perhaps the most important optimization
 - Directly reduces running time (memory access ⇒ register access)
 - Useful for other optimizations e.g. cse assumes old values are kept in registers.
- More important as processor speeds grow faster than memory speeds

- Find an assignment for all pseudo-registers, if possible.
- If there are not enough registers in the machine, choose registers to spill to memory

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Example



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II. An Abstraction for Allocation & Assignment

Intuitively

- Two pseudo-registers **interfere** if at some point in the program they cannot both occupy the same register.
- Interference graph: an undirected graph, where
 - nodes = pseudo-registers
 - there is an edge between two nodes if their corresponding pseudo-registers interfere

· What is not represented

- Extent of the interference between uses of different variables
- · Where in the program is the interference

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Register Allocation and Coloring

- A graph is n-colorable
 if every node in the graph can be colored with one of the n colors
 such that two adjacent nodes do not have the same color.
- Assigning n registers (without spilling) = Coloring with n colors
 - assign a node to a register (color) such that no two adjacent nodes are assigned same registers(colors)
- Is spilling necessary? = Is the graph n-colorable?
- To determine if a graph is n-colorable is NP-complete, for n>2
 - · Too expensive
 - Heuristics

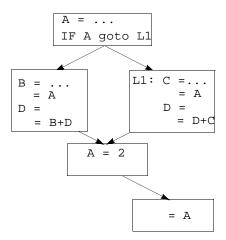
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III. Algorithm

- Step 1. Build an interference graph
 - a. refining notion of a node
 - b. finding the edges
- Step 2. Coloring
 - · use heuristics to try to find an n-coloring
 - Successful \Rightarrow colorable and we have an assignment
 - Failure ⇒ graph not colorable, or graph is colorable, but it is too expensive to color

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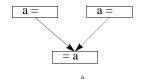
Step 1a. Nodes in an Interference Graph



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Live Ranges and Merged Live Ranges

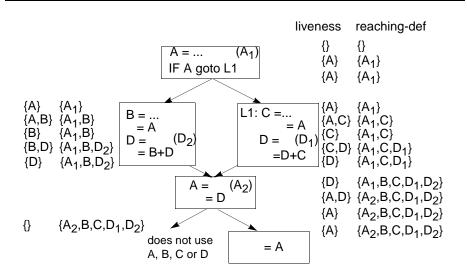
- Motivation: to create an interference graph that is easier to color
 - Eliminate interference in a variable's "dead" zones.
 - Increase flexibility in allocation: can allocate same variable to different registers
- A **live range** consists of a definition and all the points in a program (e.g. end of an instruction) in which that definition is live.
 - How to compute a live range?
- Two overlapping live ranges for same variable must be merged



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Example (revisited)



Merging Live Ranges

Merging definitions into equivalence classes

- Start by putting each definition in a different equivalence class
- · For each point in a program
 - if variable is live, and there are multiple reaching definitions for the variable
 - merge the equivalence classes of all such definitions into one equivalence class
- From now on, refer to merged live ranges simply as live ranges

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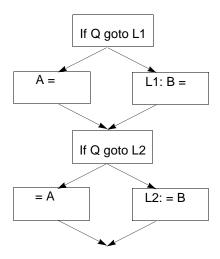
Step 1b. Edges of Interference Graph

Intuitively

- Two live ranges (necessarily of different variables) may interfere
 if they overlap at some point in the program.
- Algorithm
 - At each point in program enter an edge for every pair of live ranges at that point.

· An optimized definition&algorithm for edges:

- Algorithm: check for interference only at the start of each live range
- Faster
- Better quality



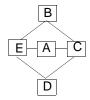
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Step 2. Coloring

- Reminder: coloring for n > 2 is NP-complete
- Observations
 - a node with degree < n ⇒
 - can always color it successfully, given its neighbors' colors
 - a node with degree = n ⇒
 - a node with degree $> n \Rightarrow$

Coloring Algorithm

- Algorithm
 - · Iterate until stuck or done
 - Pick any node with degree < n
 - Remove the node and its edges from the graph
 - If done (no nodes left)
 - · reverse the process and add colors
- Example (n = 3)

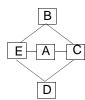


- Note: degree of a node may drop in iteration
- Avoids making arbitrary decisions that make coloring fail

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What Does Coloring Accomplish?

- Done: colorable, also obtained an assignment
- Stuck:
 - · colorable or not?



What to Do if Coloring Fails?

· Use heuristics to improve its chance of success and to spill code

Build interference graph

Iterative until there are no nodes left

If there exists a node v with less than n neighbor place v on stack to register allocate

else

v = node chosen by heuristics
 (least frequently executed, has many neighbors)
 place v on stack to register allocate (mark as spilled)
remove v and its edges from graph

While stack is not empty

Remove v from stack

Reinsert v and its edges into the graph

Assign v a color that differs from all its neighbors

(guaranteed to be possible for nodes not marked as spilled)

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Summary

- Problems:
 - · Given n registers in a machine, is spilling avoided?
 - Find an assignment for all pseudo-registers, whenever possible.
- Solution
 - · Abstraction: an interference graph
 - nodes: merged live ranges
 - · edges: presence of live range at time of definition
 - Register allocation and assignment
 - = n-colorability of interference graph
 - ⇒ NP-complete
 - Heuristics to find an assignment for n colors
 - successful: colorable, and finds assignment
 - · not successful: colorability unknown & no assignment

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